# **Event Biasing**

Geant4 PHENIICS & IN2P3 Tutorial, 16 – 20 May 2022, Orsay

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### Overview

- I. Introduction
- II. Existing Biasing Options before v10.0
  - Primary Particle Biasing
  - Options In Hadronic
  - Geometry based importance biasing
  - Weight Window Technique
  - Reverse Monte Carlo
  - User defined biasing
- III. Generic biasing (since v10.0)

# I. Introduction

# **Rare events**

- > There are simulation problems in which what we are interesting in is "rare"
  - rare because of the physics,
  - or because of the setup,
  - Etc.
- > Examples of such problems:
  - Estimating the efficiency of a shield
    - > A large flux enters a shield...
    - > ... with a lot of interactions inside, which is CPU intensive
    - ... and only a tiny fraction of particles exiting : the rare ones.

#### Obtaining the response of a very thin detector

- > For example to obtain the response to neutrons
- > Most of them do not interact in
- > But the signal is made by the rare ones which interact

#### - Estimating the dose in a very small part of a big setup

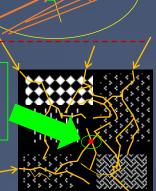
- > For example an electronic chip inside a satellite
- Most of the time is spent simulating showers that do not contribute the dose
- > While we want to tally this dose

Volume in which we want to estimate the dose

Incident flux

**Rare interactions** 

making the signal



Remaining flux we want to estimate

Thick shield/

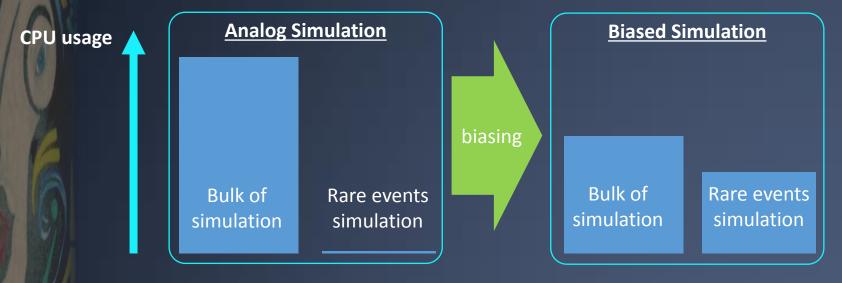
Thin detector

An "analog" (usual) simulation is very inefficient in addressing these problems.

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# What is "event biasing" ?

- "Event biasing" (or "biasing" or "variance reduction") is a set of techniques to simulate rare events efficiently
  - It is an accelerated simulation with respect to these events
    - > And to these events only : ie not everywhere !
  - It focuses/transfers the CPU power usage on what we want to tally



- It can provide LARGE CPU improvements
  - > Several orders of magnitude ! Depending on the problem.
- > "Biasing" stands for "biased simulation":
  - "Biased simulation" because rare events are enhanced compared to the analog simulation.

# Main principles

- > Enhancement of rare events is tracked with statistical "weights":
  - Weights are used to "de-bias" and go back to analog quantities:
    - > Eg:  $E_{deposit} = \sum_{i=track} weight_i \times E^i_{deposit}$



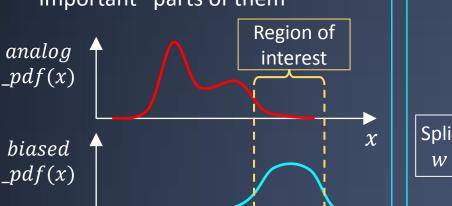
Track i, weight i

> There is a large variety of techniques (sometimes with ≠ names for ≈ techniques) but two methods make the "backbone" of most of them:

#### **Importance Sampling**

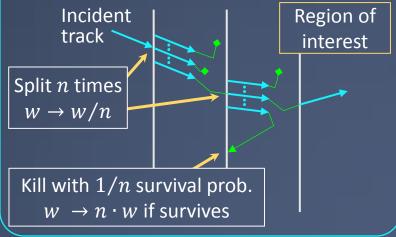
 $w(x) = \frac{analog_pdf(x)}{biased pdf(x)}$ 

 Modify physics pdf's enhancing "important" parts of them



#### Splitting (& Killing)

 Keep *pdf*'s unchanged but split (kill) when moving towards (receding from) region of interest

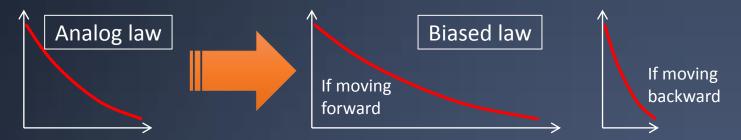


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### **Examples of importance sampling techniques**

#### > The "exponential transform" technique

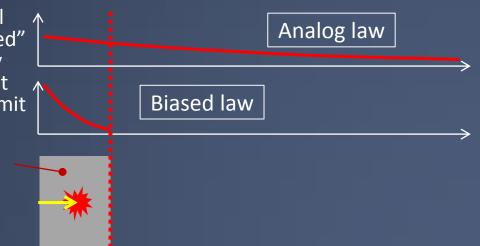
- It is a change of the total cross-section
- Often made direction dependent
- The usual/analog exponential law is replaced by an other law (still an exponential one here, but with different cross-section)



#### > Forcing the interaction in a thin volume:

 The usual/analog exponential law is replaced by a "truncated" exponential law (not the only possible choice) that does not extend beyond the volume limit

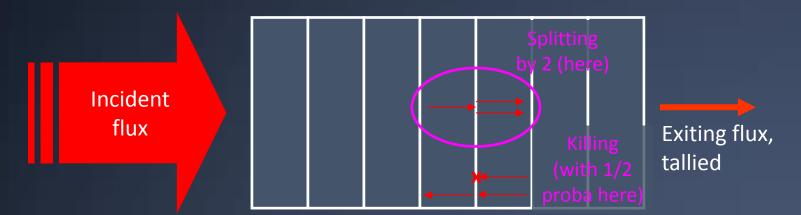
Volume in which we want the interaction to be forced



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# **Example of splitting**

> A classical application of splitting is the "shield" simulation problem



In above example, particles moving toward exit are cloned

- cloning is for compensating the physical absorption in the shield material
- When cloning happens, clones receive a weight ½ (here) of the initial track

#### Splitting comes together with « killing » / « Russian Roulette »

- For particles going opposite to want we want
- In above example, particles moving backward are killed with a (here) probability ½ and, if it survives, its weight is multiplied by 2 (here).

# Biasing versus other acceleration techniques ?

#### > Other acceleration techniques exist:

- "fast simulation" : replacement of detailed simulation by approximate but faster model (eg: EM showers)
- Deterministic computation (in some cases)

### > Interest of biasing:

- When using biasing, the physics modeling is the same than the detailed simulation one
  - > Biasing is "simply" an other way to process the full detailed physics
- So, results obtained with biasing are statistically the same than the ones obtained with a large/huge processing of standard simulation

### > Difficulties with biasing:

- Only "rare events" problems can be treated this way
- Ensuring a proper convergence can be difficult
  - > Issue of random appearance of very large weights
    - that destroy the convergence
  - This signs that parts of the problem are not sampled enough (illustration in backup slides)

# II. Existing Biasing Options before v10.0

### **Primary Particle Biasing**

- > The General Particle Source (GPS) allows to bias the particle source:
  - Position
  - Angular Distribution
  - Energy Distribution
- > This is an "importance sampling" biasing
  - The physical distributions are replaced by biased ones
- Primary particles are given a weight that is the ratio of analog / biased probabilities
  - In the simulation, all daughter, gran-daughter,... particles from the primary inherit the weight of this primary

# **Options In Hadronic (1)**

#### > Cross-section Biasing:

- Possibility to enhance a (low) cross-section
  - > This an "importance sampling" approach
- Available for photon inelastic, electron & positron nuclear processes

//init reaction model
G4ElectroNuclearReaction\* theElectroReaction = new G4ElectroNuclearReaction();

//create process and register model
G4ElectronNuclearProcess theElectronNuclearProcess;
theElectronNuclearProcess.RegisterMe(theElectroReaction);

//apply biasing
theElectronNuclearProcess.BiasCrossSectionByFactor(100);

#### //register process

pManager->AddDiscreteProcess(&theElectronNuclearProcess);

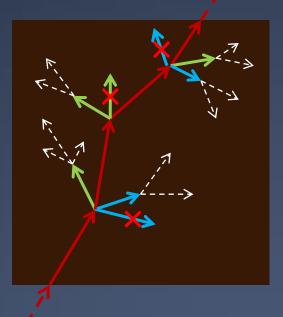
- (no messenger for this?)

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# **Options In Hadronic (2)**

### > Leading Particle Biasing:

- It is a technique used for estimating the penetration of particles in a shield
- Instead of simulating the full shower, at each interaction, only keep:
  - > The most energetic particle
  - > + randomly one particle of each species
- This is a « killing » based biasing

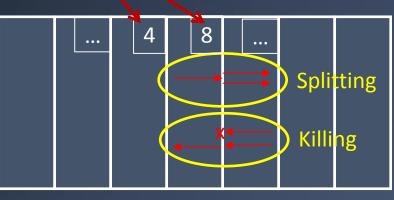


### > Radioactive decay

- Enhance particular decay within a given time window
- Sample all decay modes with equal probabilities
- Split parent nuclide in a user defined number of copies, letting the decay go
- Enhance emission in a particular direction

# **Geometry based importance biasing**

- > A direct application of what was presented earlier here
- > Attach "importance" to cells in geometry
  - Not to be confused with "importance sampling" : ie change of probability density functions of interaction laws



- Applies splitting if the track moves forward
  - > with splitting factor 8/4 = 2, if track goes from « 4 » to « 8 » (eg, here)
  - > each copy having a weight =  $\frac{1}{2}$  of the incoming track
- Applies killing if the track moves the other way
  - $\,\,$  it is killed with a probability  $^{\prime\!\!/}_{\!\!\!2}$
  - > If particle survives, its weight is multiplied by 2 (eg, here)

# **Geometry based importance biasing**

 Geometry cells, meant to carry importance values, are created and associated to physical volumes in the detector construction:

G4IStore \*istore = G4IStore::GetInstance();

// Loop on physical volumes:

Replica number, if any —

istore->AddImportanceGeometryCell(importanceValue, physicalVolumePointer [, nReplica]);

- All volumes should be given an importance value.
- Biasing may be applied to some particle type only: eg neutron. In the main program, this is specified as:

G4GeometrySampler geometrySample(worldVolume, "neutron");

- (worldVolume specified as there is the ability to define cells in a parallel geometry: not discussed here)
- The actual splitting and killing are handled by dedicated processes. These are to be inserted in the physics list. If using a modular physics, it is done as: G4VModularPhysicsList\* physicsList = new FTFP\_BERT;

physicsList->RegisterPhysics(new G4ImportanceBiasing(&geometrySampler));

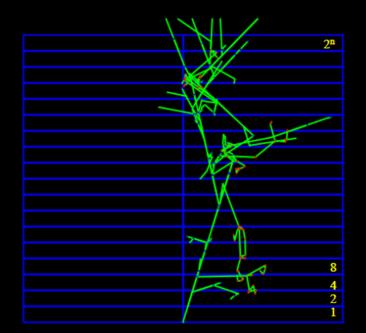
- > More details can be found in examples:
  - examples/extended/biasing/B01 : geometry biasing with importance cells or weight window
  - examples/extended/biasing/B02 : same, with cells in a parallel geometry
  - examples/extended/biasing/B03 : same, for the case of a non modular physics list

# Example B01 - 10 MeV neutrons, thick concrete cylinder

#### **Analogue Simulation**

Importance Sampled

~
/ ^
/





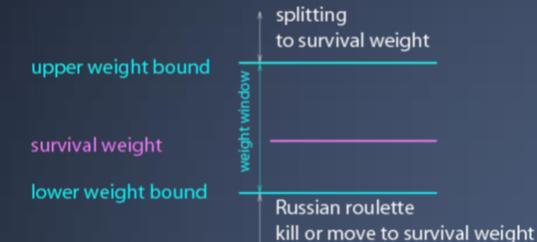
See: geant4/examples/extended/biasing/B01

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# Weight Window Technique

### > This is a « splitting & killing » technique, to avoid having

- Too high weight tracks at some point
  - > As this makes the convergence of the estimated quantities difficult
  - > Tracks with weight above some value are splitted
- Too low weight tracks
  - > As these are essentially a waste of time
  - > Tracks below some value are "Russian roulette" killed

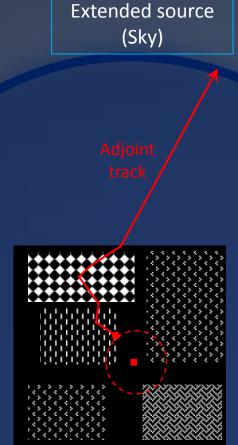


- > As with importance, this is configured per cell
  - And can be configured per energy
- > See: geant4/examples/extended/biasing/B01

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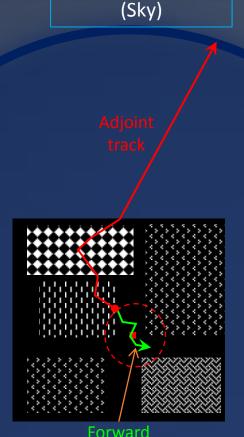
### **Reverse Monte Carlo**

- > Simulation in which particles go back in time !
- Useful in case of small device to be simulated in a big environment
  - Requested by ESA, for dose study in electronic chips in satellites
- > Simulation starts with the red track
  - So-called "adjoint" track
  - Going back in time
  - Increasing in energy
  - Up to reaching the extended source



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- > Simulation starts with the red track
  - So-called "adjoint" track
  - Going back in time
  - Increasing in energy
  - Up to reaching the extended source
- If track energy < high energy limit of the sky source spectrum</p>
  - Proceed with a usual "forward" simulation (green track)
- When many track simulated, adjust adjoint track weights so that energy spectrum of adjoint particle matches sky source spectrum
  - This provides the weight of the green tracks
- Dose in chip can then be computed, accounting for the forward track contribution, with the proper weight.
- See: geant4/examples/extended/biasing/ReverseMC01



(normal) track

**Extended** source

# **User defined biasing**

- G4WrapperProcess can be used to implement user defined event biasing
- G4WrapperProcess, which is a process itself, wraps an existing process
- > All function calls forwarded to wrapped process

#### > Needed steps:

- 1. Create derived class inheriting from G4WrapperProcess
- 2. Override only the methods to be modified, e.g., PostStepDolt()
- 3. Register this class in place of the original
- 4. Finally, register the original (wrapped) process with user class

# **Example with brem. splitting**

Bremstralhung splitting is a technique used for example in medical applications:

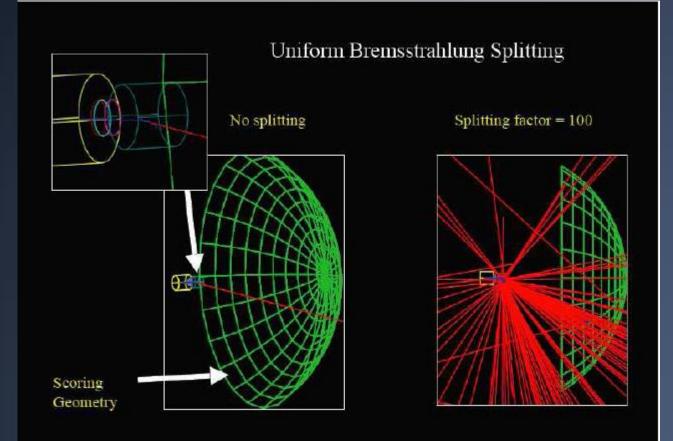
- Radio-therapy with photon beam generated by bremstralhung
- Interest is in generated photons, not in the electron  $\rightarrow$  enhance photon production
- The bremstralhung process is repeated N times, with the same initial electron
  - All bremstralhung photons are given a weight 1/N
  - The electron continues with one of the state among the N ones generated

G4VParticleChange\* myWrappedProc::PostStepDoIt(const G4Track& track, const G4Step& step) {

```
G4double weight = track.GetWeight()/fNSplit;
```

```
std::vector<G4Track*> secondaries(fNSplit);
```

# **Example with a brem. splitting**



> Note: Since 9.6, a built-in brem. splitting option is now proposed.

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# III. Generic Biasing (since v10.0)

# Why and what generic scheme ?

#### Many options existed

- But lived next to each other
  - > Each introduced its own infrastructure
  - > Making uneasy the combination of them
- No general scheme to modify the physics process behavior
  - Interaction probability
  - > Final state generation
  - > While it is a the start of many biasing techniques

#### Revise by adopting a classical "object oriented" (OO) approach:

- An abstract layer, general enough
  - > With concrete implementations deriving from it
  - > Making, as anywhere in Geant4, this abstract layer open to users
- Request this layer to handle physics process biasing + splitting and killing

#### > Try to make:

- A "modular" scheme, with re-usable components
- The user/developer having a maximum of information to make decisions
- Hoping this will favor users' creativity

# Modularity

### > Example of "force collision" scheme à la MCNP

#### Thin detector volume

Particle « cloning » at entrance

Incoming particle, weight =  $w_0$  Forced uncollided part, also called Forced Flight weight =  $w_0 e^{-\sigma L}$ 

Forced collided part, weight =  $w_0(1-e^{-\sigma L})$ Collision distance  $\ell$  sampled as:  $\sigma e^{-\sigma \ell}/(1-e^{-\sigma L})$ 

### > Approach considered:

- Instead of providing the above scheme in one go
- Consider "atomic" "biasing operations"
  - > splitting, forced free flight, forced interaction, etc.
- Compose these with a "biasing operator"
  - > that selects, step after step, the biasing operations to build the needed sequence
  - > which is interfaced with the tracking to have these operations applied

# **Main Components**

#### > G4VBiasingOperation

- An abstract class
- Can act on a physics process:
  - > By modifying its interaction law
  - By modifying its final state generation
- Can act by itself
  - > To split or randomly kill particles

#### > G4BiasingProcessInterface

- A concrete class
- Makes the interface between the tracking and G4VBiasingOperator objects
- It can:
  - > Wrap a physics process : to let G4VBiasingOperation's modifying it
  - > Wrap no process : to let G4VBiasingOperation's to do splitting and killing

#### G4VBiasingOperator

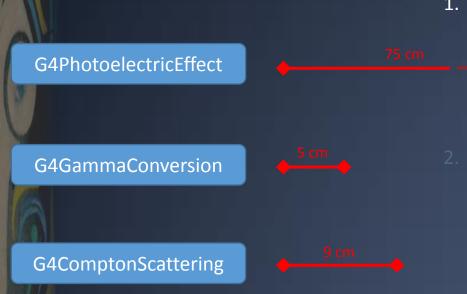
- An abstract class
- Selects G4VBiasingOperation's
  - > At the beginning of the step
  - > At the final state generation level
- This is the entity which is making all the decisions

G4BiasingProcessInterface

G4GammaConversion

## **Physics process behavior in Geant4**

#### Illustrate with point-like processes:



- 1. GetPostStepPhysicalInteractionLength()
  - Returns the distance at which the process will make an interaction
  - Analog exponential law is at play
  - Above analog behavior superseded by biased behavior (if wished)

#### . PostStepDolt()

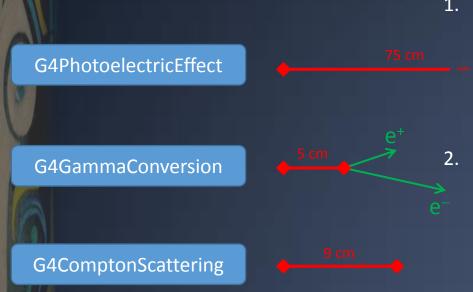
- Called if the process has responded the shortest of the interaction distances
- Generate final state, according to specific process analog physical law
- Above analog behavior superseded by biased behavior (if wished)

GABiasingProcessInterface wraps the physics process. It is meant to intercept calls for distance of interaction and for final state production.

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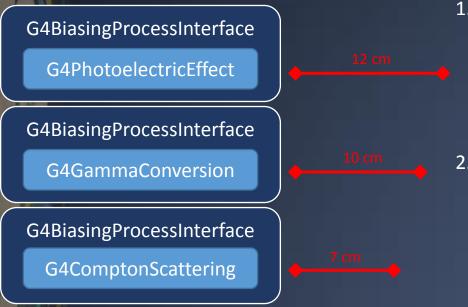
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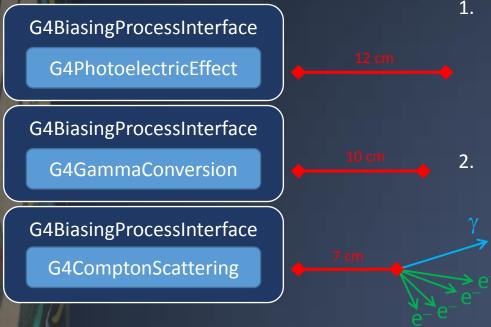
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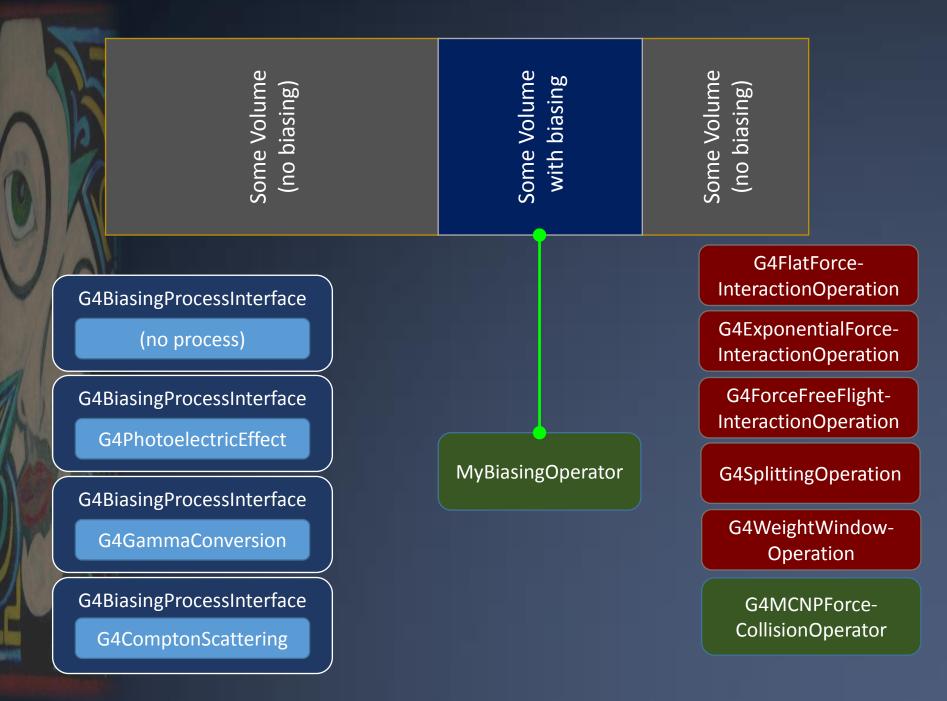


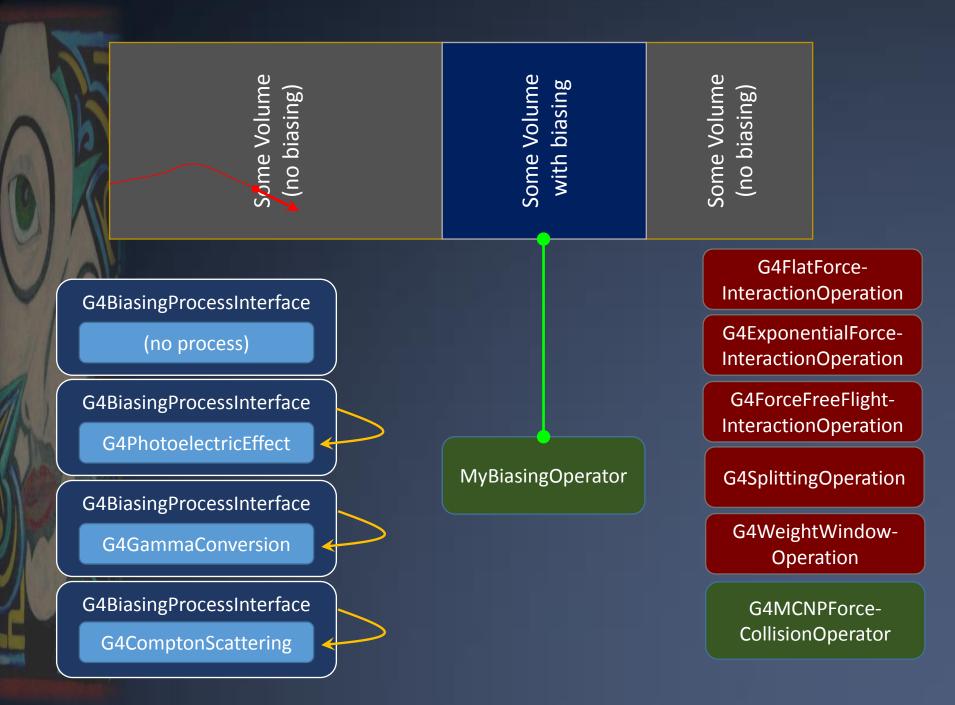
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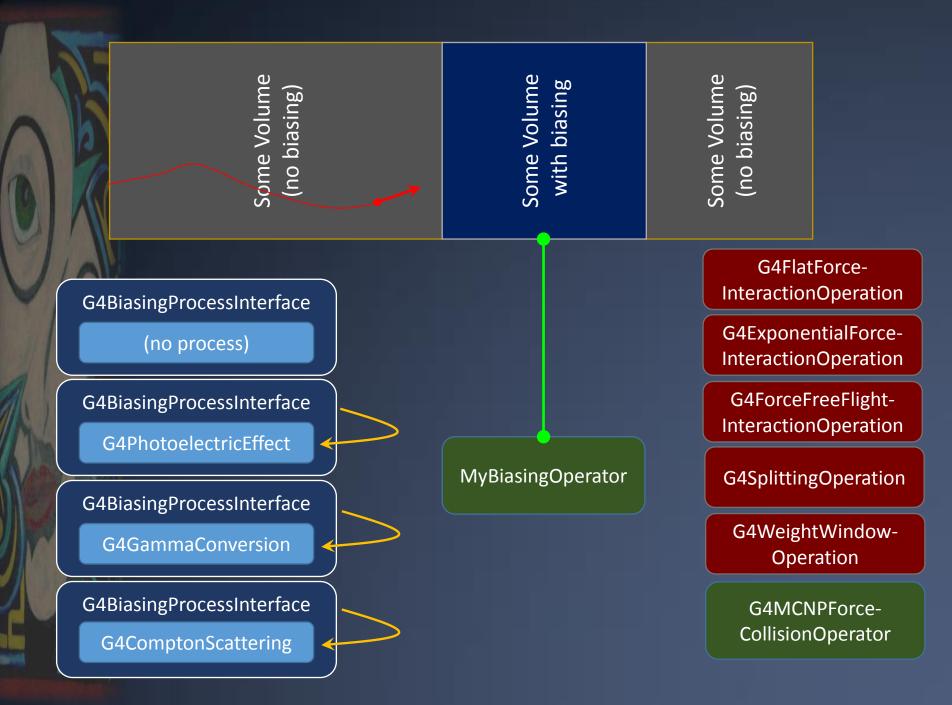
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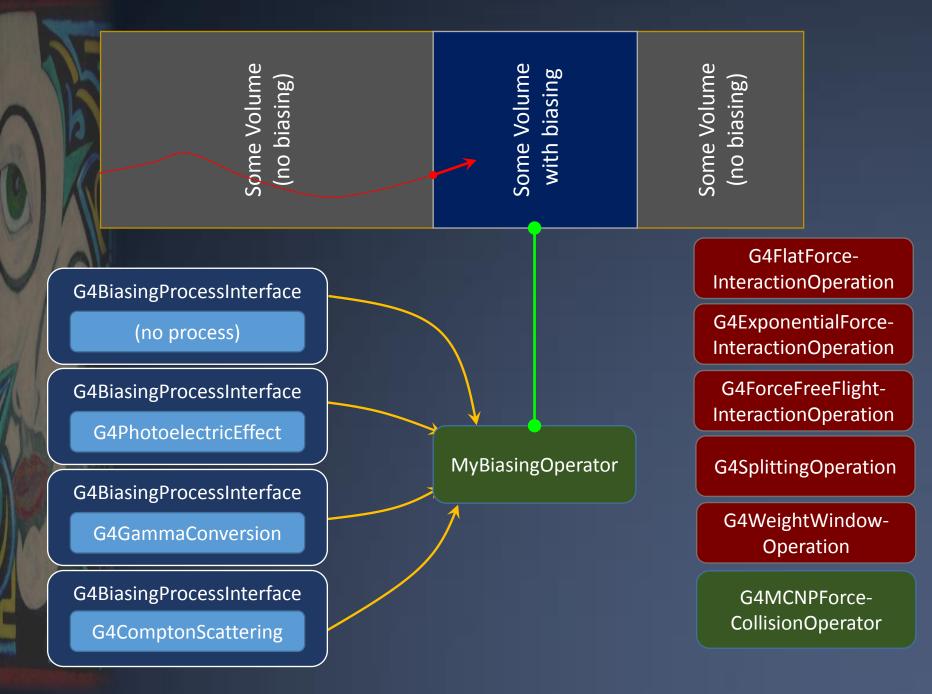
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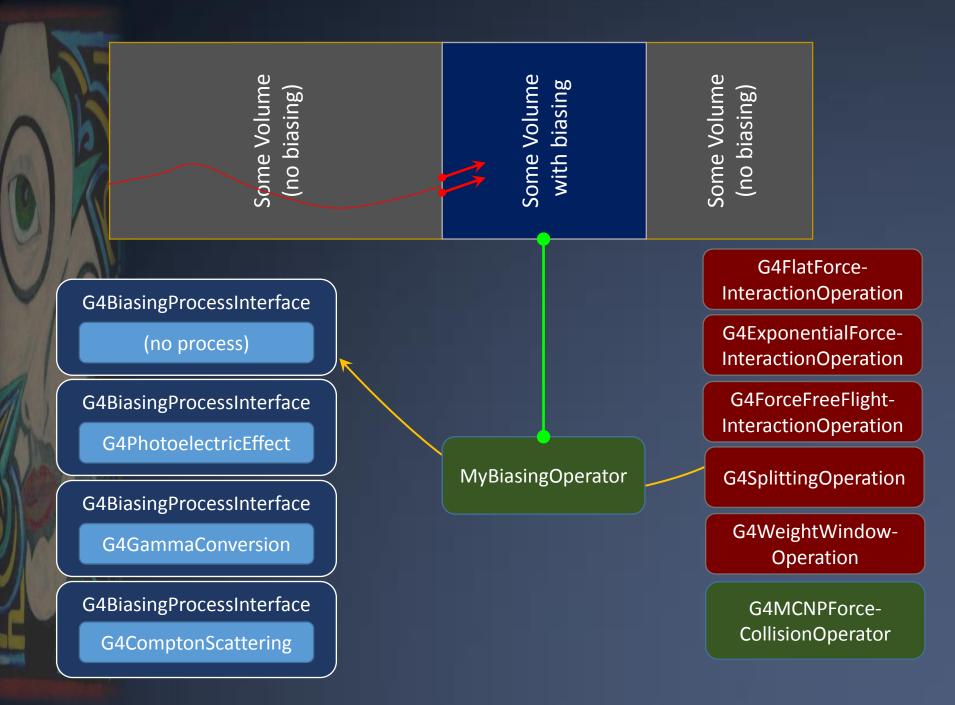




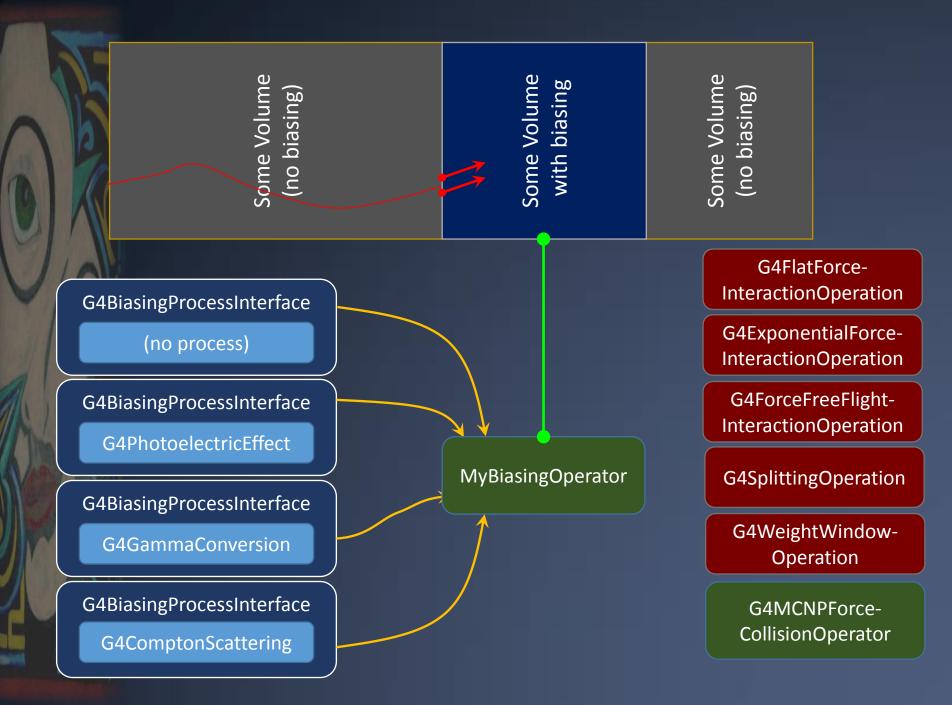


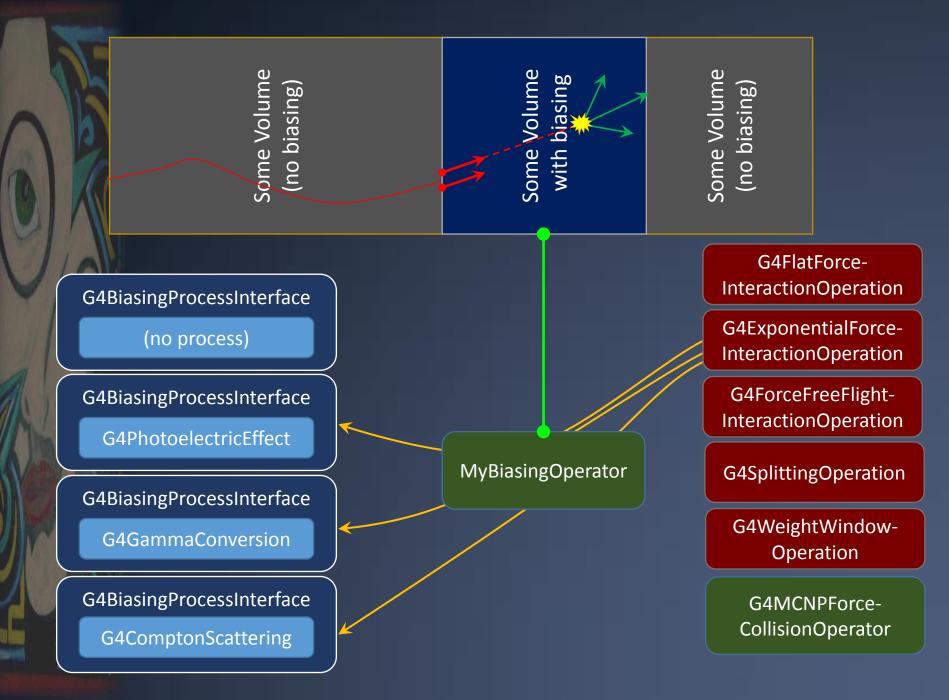


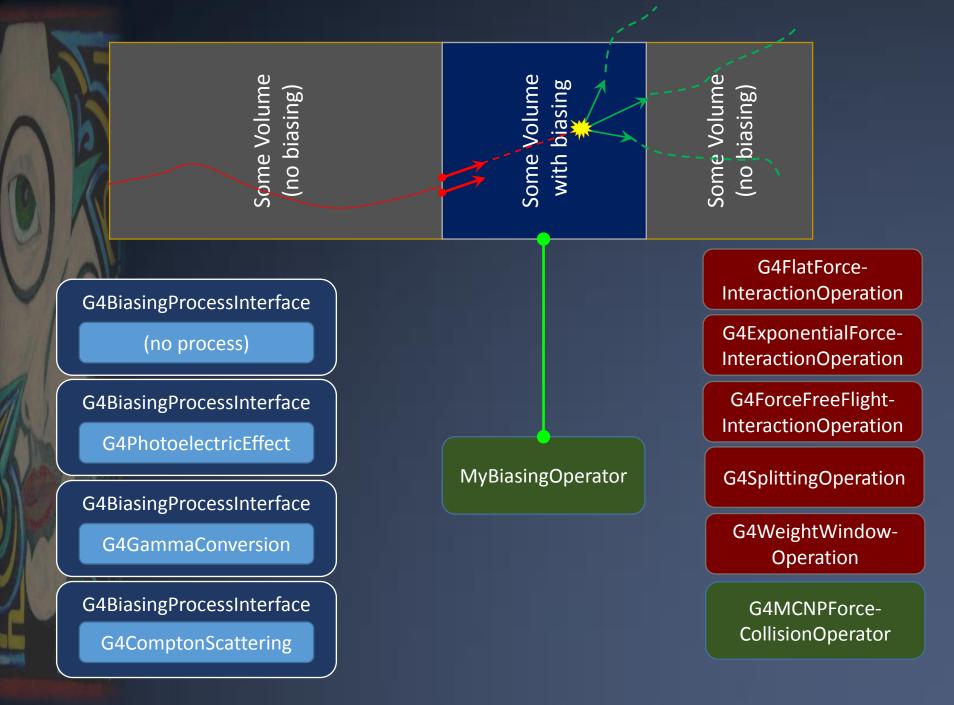
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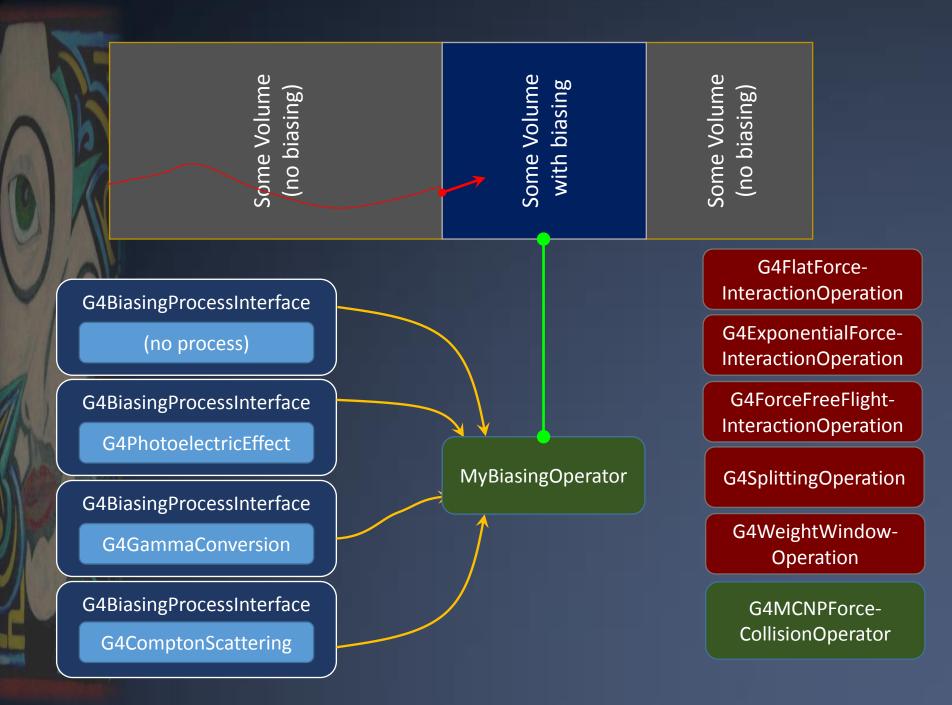


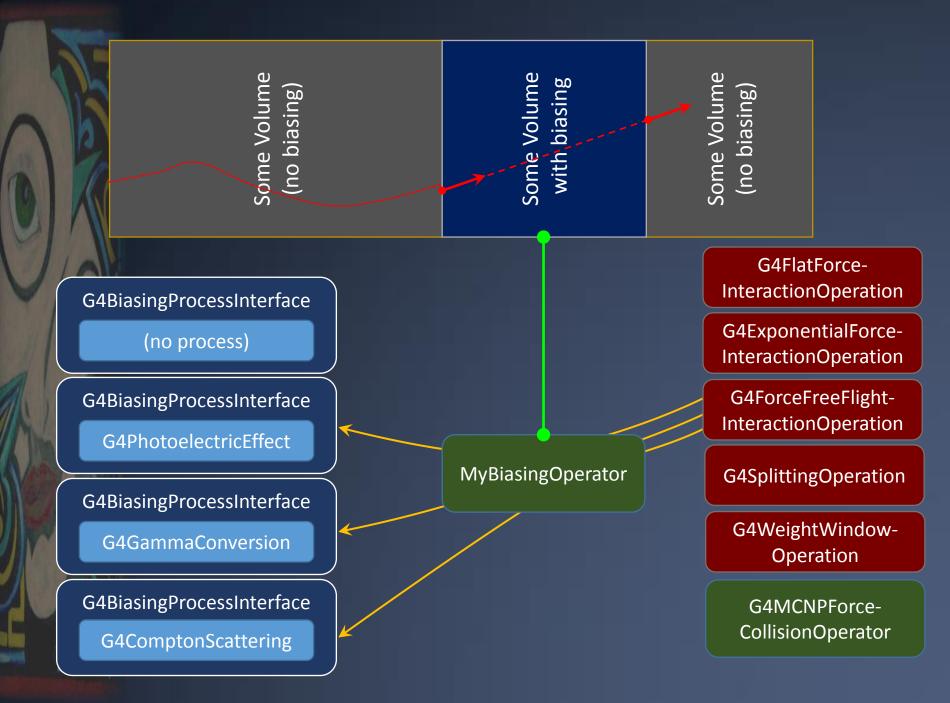
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### How to use

> In the main:

// -- Select a modular physics list FTFP\_BERT\* physicsList = new FTFP\_BERT; // -- And augment it with biasing facilities: G4GenericBiasingPhysics\* biasingPhysics = new G4GenericBiasingPhysics(); biasingPhysics->Bias("gamma"); biasingPhysics->Bias("neutron"); physicsList->RegisterPhysics(biasingPhysics); runManager->SetUserInitialization(physicsList);

- More options exist for the G4GenericBiasingPhysics constructor:
  - > Activate biasing for processes only
  - > Or for doing splitting/killing only
  - > Or to activate biasing for all charged
  - > Or all neutral particles
  - > Etc.

#### In ConstructSDandField() of detector construction:

MyBiasingOperator\* biasingOperator = new MyBiasingOperator(); biasingOperator->AttachTo( logicalVolumeToBias );

# **Existing functionalities & examples**

- > geant4/examples/extended/biasing/GB01 :
  - Individual process cross-section biasing
  - Implemented for neutral particles
  - Charged particle case requires development
    - > Issue : variation of cross-section during step because of energy loss
- > geant4/examples/extended/biasing/GB02 :
  - Force collision à la MCNP
  - Implemented for neutral particles (as MCNP)
- > geant4/examples/extended/biasing/GB03 :
  - Geometry importance + further option
  - Scheme augmented compared to classical geometry importance
    - > Allows kinds of "intermediate" non-integer splitting values
- > geant4/examples/extended/biasing/GB04 :
  - Re-implementation of a classical Bremsstrahlung splitting
- > geant4/examples/extended/biasing/GB05 :
  - Illustrates a "splitting by cross-section"
  - An invention (to my knowledge) where the splitting rate is directly adjusted from absorption cross-sections
- > geant4/examples/extended/biasing/GB06 :
  - Parallel geometries with generic biasing.

# Summary

- Biasing techniques can provide very large acceleration factors in problems in which we must tally rare events
- > Geant4 proposes biasing options
  - Primary source (GPS), leading particle, cross-section (had), radioactive decay, splitting with importance in geometry, weight window, user biasing with G4WrapperProcess, and bremstralhung splitting

#### > New "toolkit-like" approach since v10.0

- Allowing biasing of process interaction and process final state
- Together with easy mix with killing, splitting, etc.
- Introduction of base classes allows extension of functionalities et re-use of components
- > Techniques delicate to handle, but nevertheless unique in addressing rare event simulation problems.

# Backup

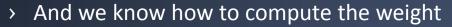
Some Words of Caution with Convergence

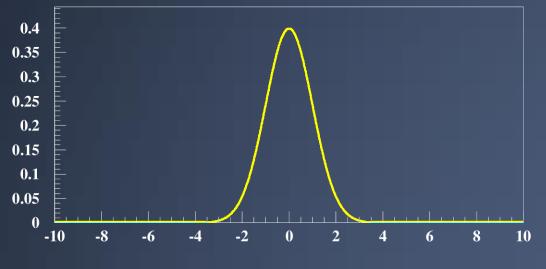
### Introduction

- Biasing techniques are powerful
  - If a technique is well suited to a problem, gains in simulation efficiency by several order of magnitudes are usual
- In contrast to an analog simulation where all "events" have the same weight (==1), biasing is not "democratic"
  - Because of the weight, some events are more important than others
- > This weight disparity may cause convergence problems
  - That can be nasty !
  - What happens is that, from time to time, an event with big weight may come, and change drastically the –say- estimated current mean value
  - Always a fear that this may happen...
- Proper convergence is the issue the user of biasing has to care about
  - And this is the price to pay for using biasing
- > Let's illustrate a "bad convergence case" with a simple problem
  - But this allows to spot the difficulties

#### Convergence

- > A « toy » example of a bad sampling:
  - We want to estimate the mean value of the unknown « yellow » distribution.
  - As we don't know where it is, we try to sample it with the « blue » distribution

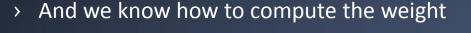


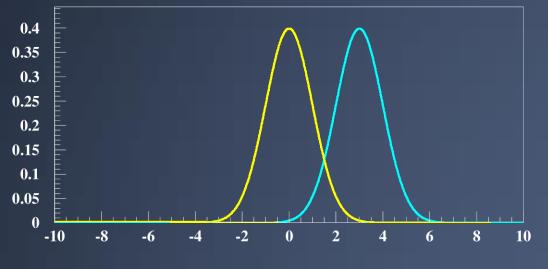


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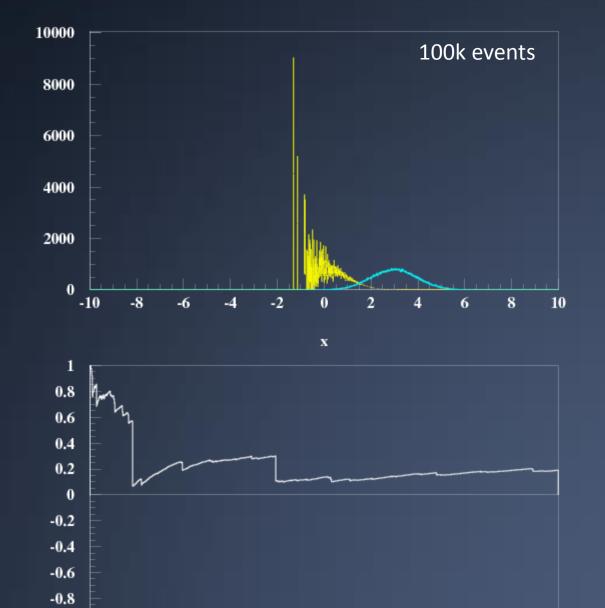
#### Convergence

- > A « toy » example of a bad sampling:
  - We want to estimate the mean value of the unknown « yellow » distribution.
  - As we don't know where it is, we try to sample it with the « blue » distribution





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Trials

6000

8000

10000

x 10

4000

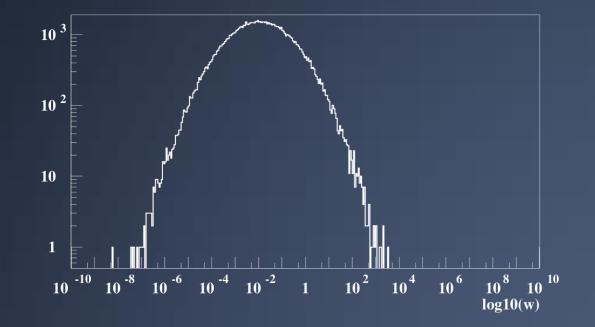
-1

0

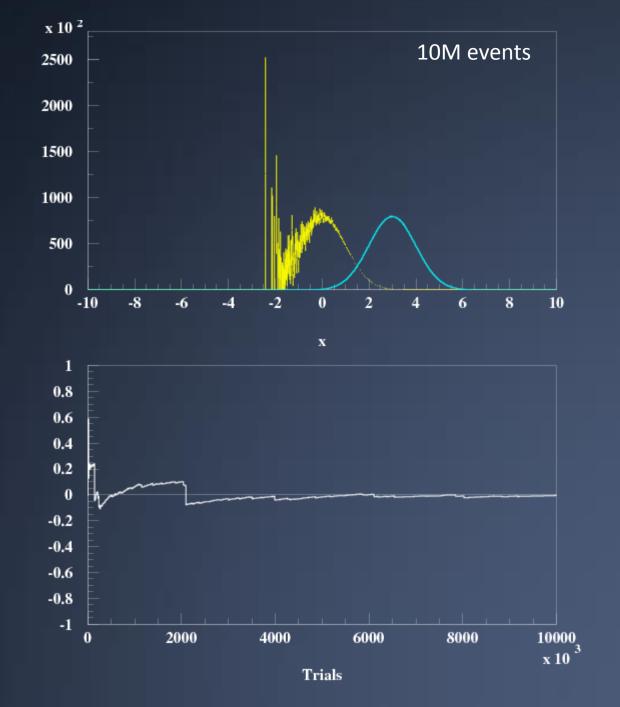
2000

### Weight distribution...

> Lots of tiny weights...



> Few huge ones...



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### Some qualitative observations

#### > Observations that can help spotting the inappropriate sampling:

- We have a wide variety of weights
  - > Many tiny ones
    - Waste of time to determine the mean value
  - > Few huge ones
    - Responsible for jumps
  - Such problem –if can not be improved- could at least be alleviated with a weight window technique
    - In a real problem (useless here in our toy problem)
- We have huge weights from time to time
  - > These are not wrong !
  - > Temptation would be to "dismiss" these events
  - > But in our case, these events bring down the mean value to the correct value
  - > These are not wrong, but *their presence is a sign of a bad sampling*
- We observe monotonic increase of the mean value
  - > We are sampling only "one side" of the problem

#### > Convergence criteria have been established in other packages

- Like MCNP

# You are invited at staying critical when using such biasing techniques !

# COMPARISON WITH FLUKA AND MCNPX

## Few words of caution

- Compare the existing FLUKA and MCNPX functionalities with the existing and planned Geant4 ones:
  - le : comparison is not exactly fair with FLUKA and MCNPX
- > Need to say the above to be fair ;)

### **FLUKA / Geant4 biasing functionalities**

Biasing options in FLUKA from http://www.fluka.org/content/manuals/fluka2011.manual		<b>Options in Geant4,</b> Present, <u>new</u> , or future
Leading particle biasing for electrons and photons: region dependent, below user- defined energy threshold and for selected physical effects.		Will be done, and will be shared with other "leading".
Russian Roulette and splitting at boundary crossing based on region relative importance.		Existing and <u>re-done with</u> g <u>eneric scheme.</u>
Region-dependent multiplicity tuning in high energy nuclear interactions.		Can be done and more general.
Region-dependent biased downscattering and non-analogue energy neutrons.	absorption of low- Simple for neutral. More	Can be done.
Biased decay length for increased daughter production.	difficult for charged but understood.	Done.
Biased inelastic nuclear interaction length.		Done.
Biased interaction lengths for electron and photon electromagnetic interactions.		Done and validated for gamma.
Biased angular distribution of decay secondary particles.		Can de done.
Region-dependent weight window in three energy ranges (and energy group dependent for low energy neutrons).		Existing. Can be "re-provided" and more general.
Bias setting according to a user-defined logics.		(need more info in FLUKA, but is actual purpose of this dev.)
User-defined neutrino direction biasing.		Can be done, easily.
User-defined step by step importance biasing.		Can be done, easily.

# **MCNPX / Geant4 biasing functionalities**

Biasing options in MCNPX From LA-UR-03-1987, MCNP5 manual	<b>Options in Geant4,</b> Present, <u>new</u> , or future	
Energy Cutoff & Time Cutoff	Existing (not considered as biasing)	
Geometry Splitting with Russian Roulette	Existing and <u>"re-provided</u> " with generic scheme.	
Energy Splitting/Roulette and Time Splitting/Roulette	Can be done easily with generic scheme.	
Weight Cutoff	Existing (in some way). Easy in generic scheme.	
Weight Window	Existing and will be "re-provided" with new design. Can be made more general.	
Exponential Transform	Done (with generic scheme).	
Implicit Capture (or "Implicit capture," "survival biasing," and "absorption by weight reduction")	Can be done. Planned for this year.	
Forced Collisions	Done (with generic scheme).	
Source Variable Biasing	Existing (GPS).	
Point Detector Tally (?)	(not biasing ?)	
DXTRAN	Planned, need more work. Doable.	
Correlated Sampling	Not planned for now "à la MCNP". But doable with user's invest.	