



Primary Particles

Geant4 PHENIICS & ANF IN2P3 Tutorial,

22 – 26 May 2023,

Orsay

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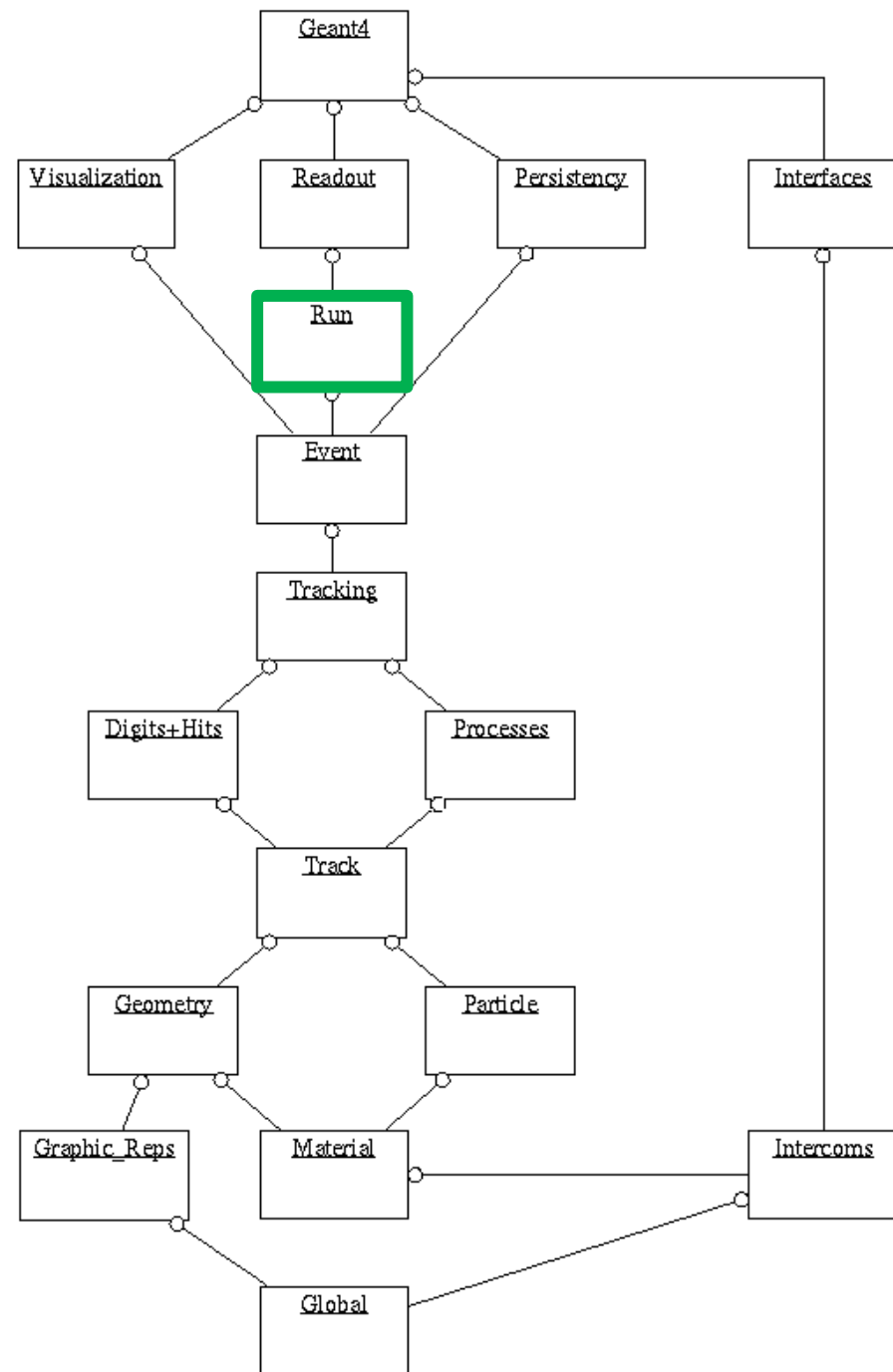
Credits...

- Filiation from at least Sébastien Incerti (CENBG), Makoto Asai, Tatsumi Koi, Dennis Wright (SLAC)
- And certainly other people !

Where will we look in the toolkit ?

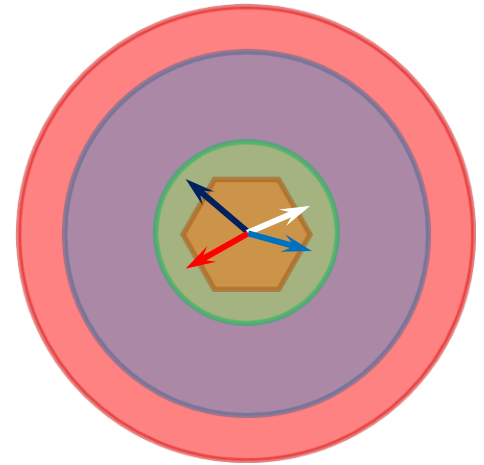
Main **category** and **directory** involved:

- **Run**
 - `geant4/source/run`



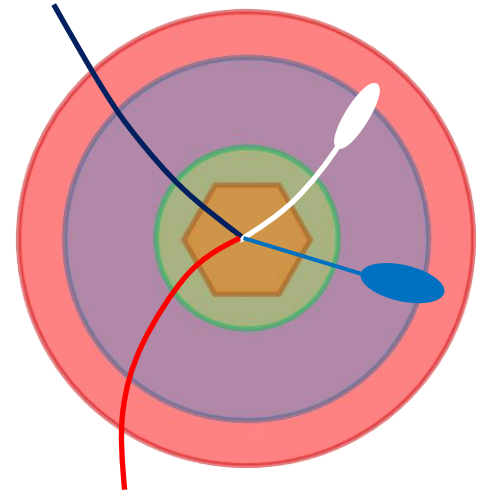
Introduction

- Here, “primary particles” stand for the particles you need to start with in your simulation at the beginning of each event:
 - For example:
 - Positrons in a PET scan imaging system in a medical application
 - Final state products in a proton-proton collision at the LHC



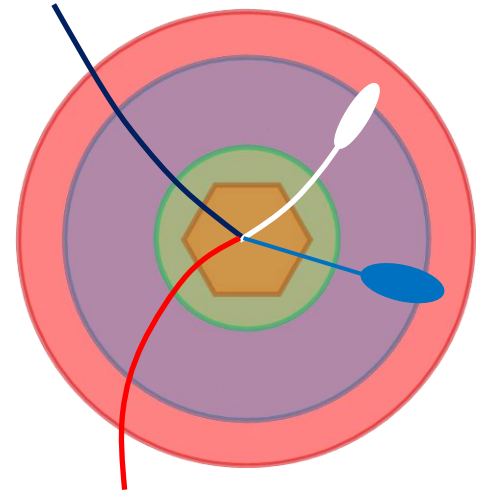
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- These particles are then transported in your geometry...
 - ... with interactions, creation of secondary particles...
 - ... and related detector response.



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 - For example:
 - Positrons in a PET scan imaging system in a medical application
 - Final state products in a proton-proton collision at the LHC
- These particles are then transported in your geometry...
 - ... with interactions, creation of secondary particles...
 - ... and related detector response.
- The primary particles must be particles that Geant4 is able to track:
 - I.e. : don't ask Geant4 for tracking a Higgs boson or a SUSY particle !
 - Unless you have extended yourself the physics of Geant4 to do so...
 - But provide instead the decay products of these:
 - Eg : particles resulting from hadronisation of $b\bar{b}$... or decays of ZZ in case of a Higgs, etc.
- You have to produce these primary particles taking some action
 - It is explained here how.



A mandatory operation

- Defining this action to produce “primary particles” is one of the three **mandatory** operations you have to do to make a working simulation.
 - Remember the two other mandatory operations:
 - detector construction: inheriting from **G4VUserDetectorConstruction**
 - physics list: inheriting from **G4VUserPhysicsList**

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- To take effect, a MyPrimaryGeneratorAction object must be passed to the runManager:

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- You define this action inheriting from the **G4VUserPrimaryGeneratorAction** base class:
 - Let’s call your concrete class “MyPrimaryGeneratorAction”
- To take effect, a MyPrimaryGeneratorAction object must be passed to the runManager:

- **In your action initialization class:**

```
void MyActionInitialization::Build() const
```

```
{
```

```
    SetUserAction(new MyPrimaryGeneratorAction);
```

```
}
```

- **And in your main program:**

```
runManager->SetUserInitialization(new MyActionInitialization);
```

```
{ G4RunManager* runManager = new G4RunManager;
```

```
or
```

```
G4MTRunManager* runManager = new G4MTRunManager;
```

- if Geant4 version < Geant4 v10.0 (obsoleting):

- **In your main program:**

```
runManager->SetUserAction(new MyPrimaryGeneratorAction); [Kept > v10.0 for backward compatibility]
```

```
{ G4RunManager* runManager = new G4RunManager;
```

A mandatory operation

- Defining this action to produce “primary particles” is one of the three **mandatory** operations you have to do to make a working simulation.
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- You define this action inheriting from the **G4VUserPrimaryGeneratorAction** base class:
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- **In your action initialization class:**

```
void MyActionInitialization::Build() const
{
    SetUserAction(new MyPrimaryGeneratorAction);
}
```

- **And in your main program:**

```
runManager->SetUserInitialization(new MyActionInitialization);
```

```
{ G4RunManager* runManager = new G4RunManager;
  or
  G4MTRunManager* runManager = new G4MTRunManager;
```

- if Geant4 version < Geant4 v10.0 (obsoleting):

- **In your main program:**

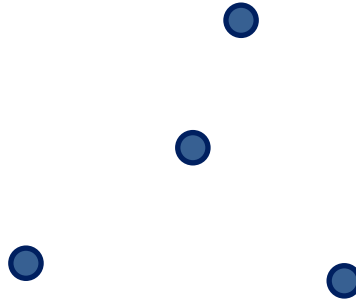
```
runManager->SetUserAction(new MyPrimaryGeneratorAction); [Kept > v10.0 for backward compatibility]
```

- During the event loop, this action will be invoked at the **beginning of each event**.
 - This invocation defines the start of the event.

Primary particle generation, in principle

- For each event, you will define:

G4PrimaryVertex objects
= {position, time}

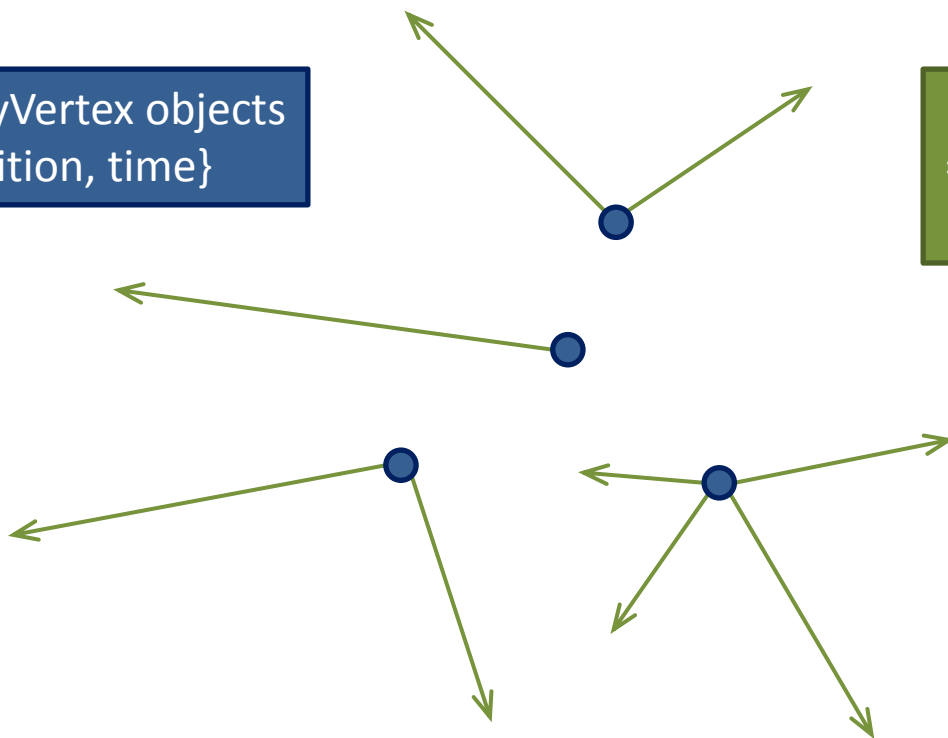


Primary particle generation, in principle

- For each event, you will define:

G4PrimaryVertex objects
= {position, time}

G4PrimaryParticle objects
= {PDG, mass, momentum,
polarization...}

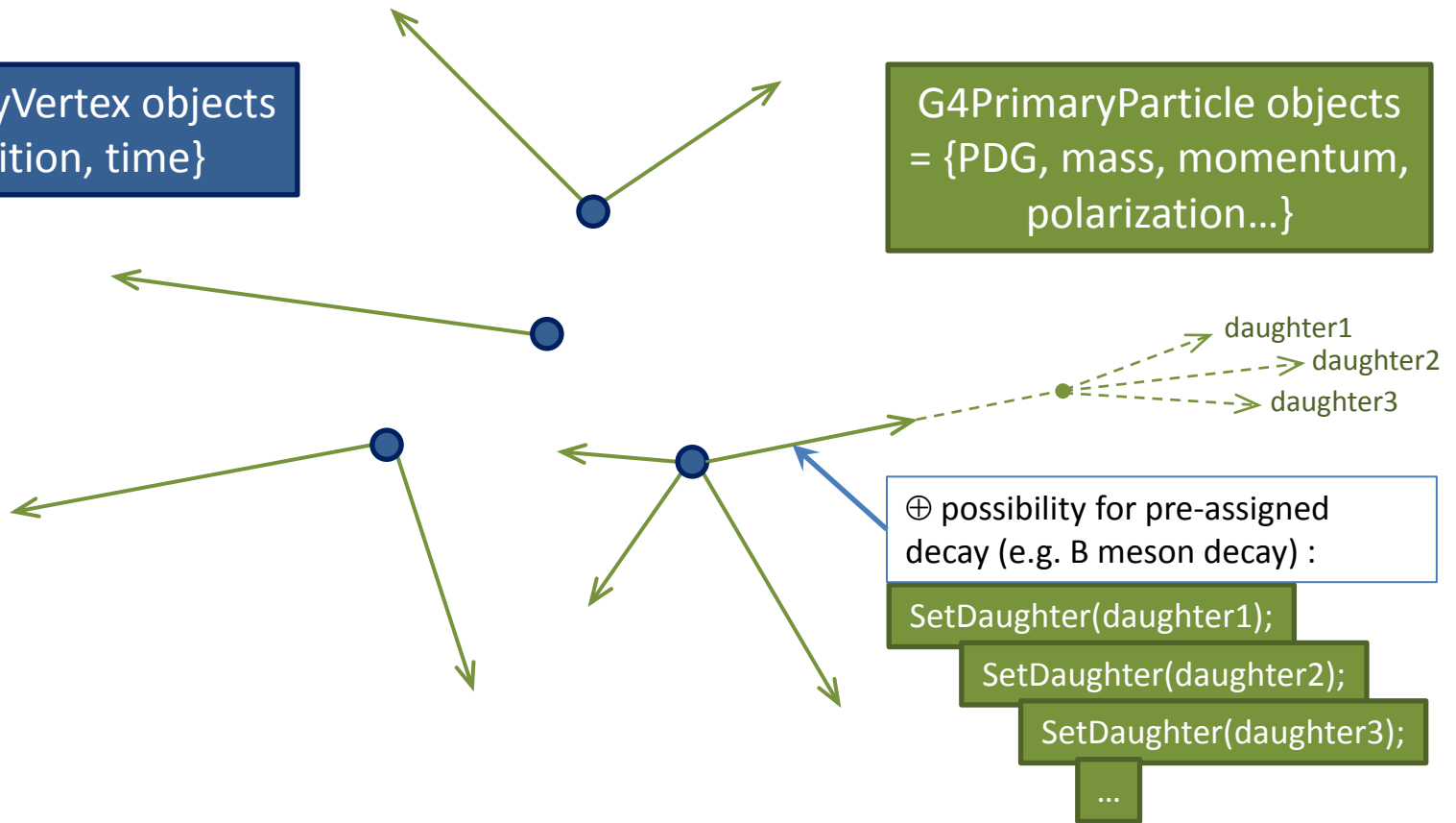


Primary particle generation, in principle

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G4PrimaryVertex objects
= {position, time}

G4PrimaryParticle objects
= {PDG, mass, momentum,
polarization...}



Primary particle generation, in practice (1/2)

- Primary particle generation is made by your concrete class, inheriting from base class:

G4VUserPrimaryGeneratorAction

- The (pure virtual) method you must implement is
void GeneratePrimaries(G4Event* event);
- In this method, you pass to “event” the G4PrimaryVertex objects you created,
 - to which you have attached the related G4PrimaryParticle objects.
- This is the method called at the beginning of each event.

First example of a G4VUserPrimaryGeneratorAction, with today's sample code

```
void EDPrimaryGeneratorAction::GeneratePrimaries(G4Event* event)
{
    // Define particle properties
    G4String particleName = "proton";
    G4ThreeVector position(0, 0, -9.*m);
    G4ThreeVector momentum(0, 0, 1.*GeV);
    G4double time = 0;

    // Get particle definition from G4ParticleTable
    G4ParticleTable* particleTable = G4ParticleTable::GetParticleTable();
    G4ParticleDefinition* particleDefinition = particleTable->FindParticle(particleName);
    if ( ! particleDefinition ) {
        G4cerr << "Error: " << particleName << " not found in G4ParticleTable" << G4endl;
        exit(1);
    }

    // Create primary particle
    G4PrimaryParticle* primaryParticle = new G4PrimaryParticle(particleDefinition);
    primaryParticle->SetMomentum(momentum.x(), momentum.y(), momentum.z());
    primaryParticle->SetMass(particleDefinition->GetPDGMass());
    primaryParticle->SetCharge( particleDefinition->GetPDGCharge());

    // Create vertex
    G4PrimaryVertex* vertex = new G4PrimaryVertex(position, time);
    vertex->SetPrimary(primaryParticle);
    event->AddPrimaryVertex(vertex);
}
```


Primary particle generation, in practice (2/2)

- Primary particle generation is made by your concrete class, inheriting from base class:

G4VUserPrimaryGeneratorAction

- The (pure virtual) method you must implement is
void GeneratePrimaries(G4Event* event);
- In this method, you pass to “event” the G4PrimaryVertex objects you created,
 - to which you have attached the related G4PrimaryParticle objects.
- This is the method called at the beginning of each event.

- In practice, actual vertices and particles creation is **delegated to an other class**

G4VPrimaryGenerator

- **Very recommended**, as this makes easy re-use of code for generating primary particles
 - And several concrete implementations of these exist in Geant4 (see after)
- From G4VPrimaryGenerator, you may either
 - Inherit to implement your own, implementing the method
void GeneratePrimaryVertex(G4Event* event);
 - Or use some of the existing concrete helper implementations (details later):
 - G4ParticleGun, G4GeneralParticleSource, G4SingleParticleSource, G4HEPEvtInterface

2nd example of a G4VUserPrimaryGeneratorAction, using a G4VPrimaryGenerator : G4ParticleGun (1/2)

```
void G4ParticleGun::GeneratePrimaryVertex(G4Event* evt)
```

```
{  
    if(particle_definition==0) return;
```

```
    // create a new vertex
```

```
    G4PrimaryVertex* vertex = new G4PrimaryVertex(particle_position,particle_time);
```

```
    // create new primaries and set them to the vertex
```

```
    G4double mass = particle_definition->GetPDGMass();
```

```
    for( G4int i=0; i<NumberOfParticlesToBeGenerated; i++ ){
```

```
        G4PrimaryParticle* particle = new G4PrimaryParticle(particle_definition);
```

```
        particle->SetKineticEnergy( particle_energy );
```

```
        particle->SetMass( mass );
```

```
        particle->SetMomentumDirection( particle_momentum_direction );
```

```
        particle->SetCharge( particle_charge );
```

```
        particle->SetPolarization(particle_polarization.x(), particle_polarization.y(), particle_polarization.z());
```

```
        vertex->SetPrimary( particle );
```

```
    }
```

```
    evt->AddPrimaryVertex( vertex );
```

```
}
```

Sample code of G4ParticleGun class.
It is defined in geant4 : you don't have to provide it ! But just use it (see after).

2nd example of a G4VUserPrimaryGeneratorAction, using a G4VPrimaryGenerator : G4ParticleGun (2/2)

Constructor (ie, called once)

```
MyPrimaryGeneratorAction::MyPrimaryGeneratorAction()
```

```
{  
    G4int n_ class MyPrimaryGeneratorAction : public G4VUserPrimaryGeneratorAction  
    fparticleGun = new G4ParticleGun(n_particle);  
  
    // default particle kinematic  
    G4ParticleTable* particleTable = G4ParticleTable::GetParticleTable();  
    G4ParticleDefinition* particle = particleTable->FindParticle("gamma");  
    fparticleGun->SetParticleDefinition(particle);  
    fparticleGun->SetParticleMomentumDirection(G4ThreeVector(0.,0.,1.));  
    fparticleGun->SetParticleEnergy(100.*MeV);  
    fparticleGun->SetParticlePosition(G4ThreeVector(0.,0.,-50*cm));  
}
```

```
void MyPrimaryGeneratorAction::GeneratePrimaries(G4Event* anEvent)  
{  
    fparticleGun->GeneratePrimaryVertex(anEvent);  
}
```

2nd example of a G4VUserPrimaryGeneratorAction, using a G4VPrimaryGenerator : G4ParticleGun (2/2)

Constructor (ie, called once)

```
MyPrimaryGeneratorAction::MyPrimaryGeneratorAction()
```

```
{
```

```
    G4int n_particle = 1;
```

```
    fparticleGun = new G4ParticleGun(n_particle);
```

```
    // default particle kinematic
```

```
    G4ParticleTable* particleTable = G4ParticleTable::GetParticleTable();
```

```
    G4ParticleDefinition* particle = particleTable->FindParticle("gamma");
```

```
    fparticleGun->SetParticleDefinition(particle);
```

```
    fparticleGun->SetParticleMomentumDirection(G4ThreeVector(0.,0.,1.));
```

```
    fparticleGun->SetParticleEnergy(100.*MeV);
```

```
    fparticleGun->SetParticlePosition(G4ThreeVector(0.,0.,-50*cm));
```

```
}
```

G4ParticleGun: public G4VPrimaryGenerator

```
void MyPrimaryGeneratorAction::GeneratePrimaries(G4Event* anEvent)
```

```
{
```

```
    fparticleGun->GeneratePrimaryVertex(anEvent);
```

```
}
```

2nd example of a G4VUserPrimaryGeneratorAction, using a G4VPrimaryGenerator : G4ParticleGun (2/2)

Constructor (ie, called once)

```
MyPrimaryGeneratorAction::MyPrimaryGeneratorAction()
```

```
{
```

```
    G4int n_particle = 1;
```

```
    fparticleGun = new G4ParticleGun(n_particle);
```

```
    // default particle kinematic
```

```
    G4ParticleTable* particleTable = G4ParticleTable::GetParticleTable();
```

```
    G4ParticleDefinition* particle = particleTable->FindParticle("gamma");
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```
    fparticleGun->SetParticleDefinition(particle);
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```
    fparticleGun->SetParticleMomentumDirection(G4ThreeVector(0.,0.,1.));
```

```
    fparticleGun->SetParticleEnergy(100.*MeV);
```

```
    fparticleGun->SetParticlePosition(G4ThreeVector(0.,0.,-50*cm));
```

```
}
```

Initialization of this G4ParticleGun for shooting a same initial gamma (same E, from same \vec{x} , \vec{p} ...)

```
void MyPrimaryGeneratorAction::GeneratePrimaries(G4Event* anEvent)
```

```
{
```

```
    fparticleGun->GeneratePrimaryVertex(anEvent);
```

```
}
```

2nd example of a G4VUserPrimaryGeneratorAction, using a G4VPrimaryGenerator : G4ParticleGun (2/2)

Constructor (ie, called once)

```
MyPrimaryGeneratorAction::MyPrimaryGeneratorAction()
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    G4int n_particle = 1;
    fparticleGun = new G4ParticleGun(n_particle);

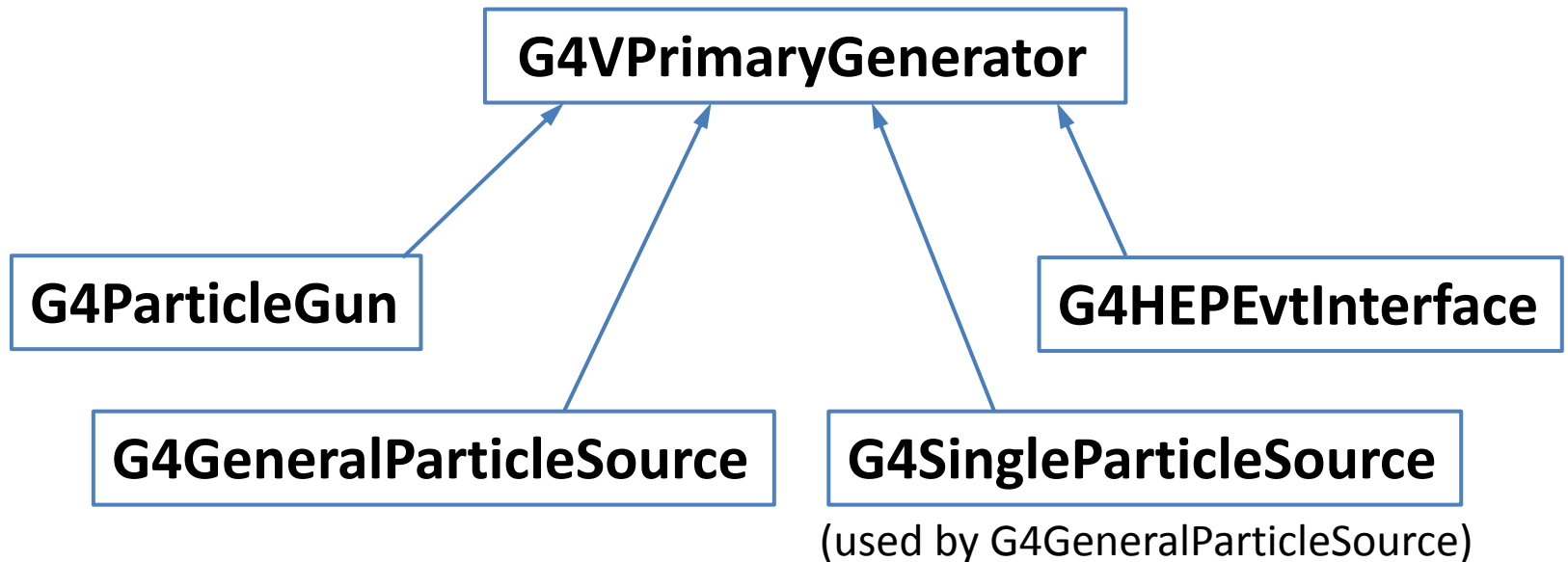
    // default particle kinematic
    G4ParticleTable* particleTable = G4ParticleTable::GetParticleTable();
    G4ParticleDefinition* particle = particleTable->FindParticle("gamma");
    fparticleGun->SetParticleDefinition(particle);
    fparticleGun->SetParticleMomentumDirection(G4ThreeVector(0.,0.,1.));
    fparticleGun->SetParticleEnergy(100.*MeV);
    fparticleGun->SetParticlePosition(G4ThreeVector(0.,0.,-50*cm));
}
```

Called at each event start

```
void MyPrimaryGeneratorAction::GeneratePrimaries(G4Event* anEvent)
{
    fparticleGun->GeneratePrimaryVertex(anEvent);
}
```

Built-in G4VPrimaryGenerator classes

- Geant4 provides concrete implementations for G4VPrimaryGenerator:



G4ParticleGun

- **The simplest G4VPrimaryGenerator implementation:**

- Shoot one or several particle(s) at a time,
- All of same fixed type, energy, momentum direction, position, time, etc.

- Particle gun configured with methods:

SetNumberOfParticles(G4int)	SetParticleEnergy(G4double)
SetParticleDefinition(G4ParticleDefinition*)	SetParticleTime(G4double)
SetParticleMomentum(G4ParticleMomentum)	SetParticlePosition(G4ThreeVector)
SetParticleMomentumDirection(G4ThreeVector)	SetParticlePolarization(G4ThreeVector)

- **Simple, and a convenient tool to start with, and that can be used for more advanced and randomized generation (and example after).**

- **G4ParticleGun comes together with a messenger** (it creates it):

- Meaning that once you have created a G4ParticleGun object in memory, its messenger is also created, and you have access interactively to the menu:
Idle > /gun/
- With commands like: /gun/energy 10 MeV ; /gun/direction 0 0 1 ; etc...
- You then just need to have the simple GeneratePrimaryVertex(anEvent) call in your `MyPrimaryGeneratorAction::GeneratePrimaries(G4Event* anEvent)` , all the configuration of the particle gun will be done interactively.

Example with randomizing a direction

- Our first simple example: shooting a gamma, with particleGun fully configured in constructor of MyPrimaryGeneratorAction:

```
void MyPrimaryGeneratorAction::GeneratePrimaries(G4Event* anEvent)
{
    fparticleGun->GeneratePrimaryVertex(anEvent);
}
```

Note: case you can all configure your particle gun interactively

- An example of e^+e^- generation, with random direction (assumes the rest is configured in MyPrimaryGeneratorAction constructor or interactively) :

```
void MyPrimaryGeneratorAction::GeneratePrimaries(G4Event* anEvent)
{
    // shoot one electron (ie: add one electron to anEvent):
    fparticleGun->SetParticleDefinition(G4Electron::Definition());
    fparticleGun->SetParticleMomentum(G4RandomDirection());
    fparticleGun->GeneratePrimaryVertex(anEvent);
    // shoot one positron (ie: add one positron to anEvent):
    fparticleGun->SetParticleDefinition(G4Positron::Definition());
    fparticleGun->SetParticleMomentum(G4RandomDirection());
    fparticleGun->GeneratePrimaryVertex(anEvent);
}
```

An other example, more granular

- Previous example was generating particles uniformly in full angular space.
- If you need to focus the production in some angular space (not uniform here), you may do something like:

```
void MyPrimaryGeneratorAction::GeneratePrimaries(G4Event* anEvent)
{
    // shoot one electron (ie: add one electron to anEvent):
    fparticleGun->SetParticleDefinition(G4Electron::Definition());
    G4double dtheta = 10.*deg;
    G4double dphi   = 25.*deg;
    G4double theta  = G4UniformRand()*dtheta;
    G4double phi    = G4UniformRand()*dphi;
    G4ThreeVector randomDirection(sin(theta)*sin(phi),
                                  sin(theta)*cos(phi),
                                  cos(theta));
    fParticleGun->SetParticleMomentumDirection(randomDirection);
    fparticleGun->GeneratePrimaryVertex(anEvent);
}
```

G4GeneralParticleSource (GPS)

- A more advanced implementation of G4VPrimaryGenerator
- It uses G4SingleParticleSource
 - Itself a G4VPrimaryGenerator
 - And which is an extended version of G4ParticleGun, allowing particles to be shoot according to distributions
- GPS Relies on the concept of “source”
 - The source emits the primary particles;
 - Of a given particle type
 - Sources can be combined with relative intensities to form a more advanced source.
 - Eg: built an Am/Be neutron + gamma source
- A source emits primary particles randomly according to
 - Position distribution
 - Ie the “source” distribution (point-like, surface, 3D...)
 - Energy, angular spectra
 - Built-in (uniform, exponential, gaussian, etc.)
 - Or user defined (providing an histogram-like data)
- Sources can be biased to enhance some phase space regions
 - And related statistical weight is provided

G4GeneralParticleSource (GPS)

- Using the GPS in your primary generator action:

```
MyPrimaryGeneratorAction::PrimaryGeneratorAction()
{
    fgps = new G4GeneralParticleSource();
}

void MyPrimaryGeneratorAction::GeneratePrimaries(G4Event* anEvent)
{
    fgps->GeneratePrimaryVertex(anEvent);
}
```

- As for the G4ParticleGun, GPS comes together with a messenger, which commands are under:

Idle > /gps/

- Which has a *rich* set of commands
- All details can be found at:

<https://geant4-userdoc.web.cern.ch/UsersGuides/ForApplicationDeveloper/html/GettingStarted/generalParticleSource.html>

geant4/examples/extended/eventgenerator/exgps/macros/ test1.g4mac : GPS Command Example 1

Macro file commands:

`/gps/particle proton`

`/gps/pos/type Point`

`/gps/pos/centre 1. 2. 1. cm`

`/gps/ang/type iso`

`/gps/energy 2. MeV`

Shooting protons

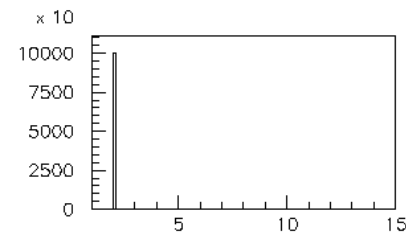
Point-like source

Source position

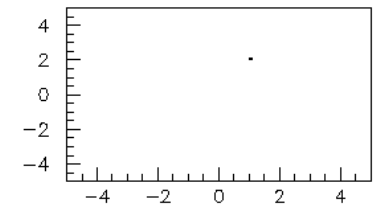
Isotropic source

Protons energy

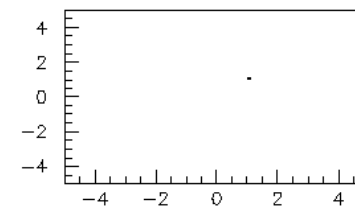
Resulting distributions



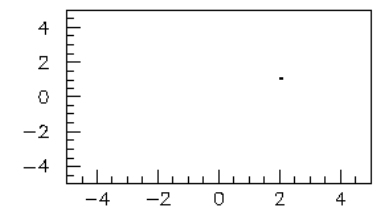
Source Energy Spectrum



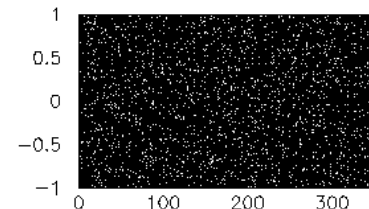
Source X-Y distribution



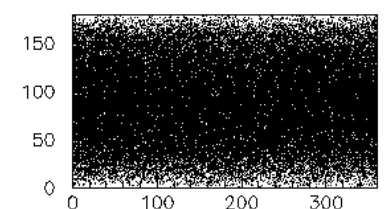
Source X-Z distribution



Source Y-Z distribution



Source cos(theta)-phi distribution



Source theta/phi distribution

geant4/examples/extended/eventgenerator/exgps/macros/ test31.g4mac : GPS Command Example 31

two beams in a generator

#

beam #1

default intensity is 1 now change to 5.

/gps/source/intensity 5.

#

/gps/particle proton

/gps/pos/type Beam

#

the incident surface is in the y-z plane

/gps/pos/rot1 0 1 0

/gps/pos/rot2 0 0 1

#

the beam spot is centered at the origin and is of

1d gaussian shape with a 1 mm central plateau

/gps/pos/shape Circle

/gps/pos/centre 0. 0. 0. mm

/gps/pos/radius 1. mm

/gps/pos/sigma_r .2 mm

#

the beam is travelling along the X_axis with

5 degrees dispersion

/gps/ang/rot1 0 0 1

/gps/ang/rot2 0 1 0

/gps/ang/type beam1d

/gps/ang/sigma_r 5. deg

#

the beam energy is in gaussian profile

centered at 400 MeV

/gps/ene/type Gauss

/gps/ene/mono 400 MeV

/gps/ene/sigma 50. MeV

(macro continuation...)

beam #2

2x the intensity of beam #1

/gps/source/add 10.

#

this is a electron beam

/gps/particle e-

/gps/pos/type Beam

it beam spot is of 2d gaussian profile

with a 1x2 mm2 central plateau

it is in the x-y plane centred at the origin

/gps/pos/centre 0. 0. 0. mm

/gps/pos/halfx 0.5 mm

/gps/pos/halfy 1. mm

/gps/pos/sigma_x 0.1 mm

the spread in y direction is stronger

/gps/pos/sigma_y 0.2 mm

#

#the beam is travelling along -Z_axis

/gps/ang/type beam2d

/gps/ang/sigma_x 2. deg

/gps/ang/sigma_y 1. deg

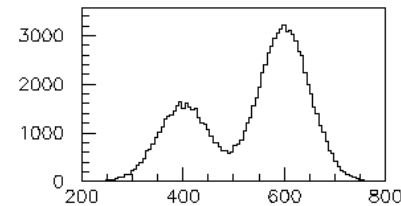
gaussian energy profile

/gps/ene/type Gauss

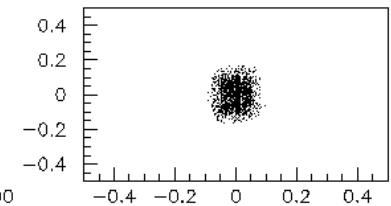
/gps/ene/mono 600 MeV

/gps/ene/sigma 50. MeV

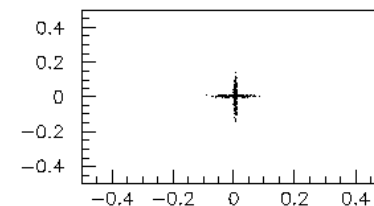
Resulting distributions



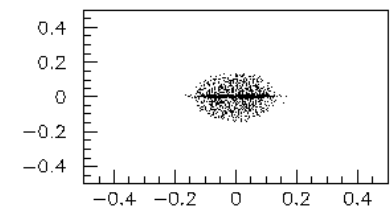
Source Energy Spectrum



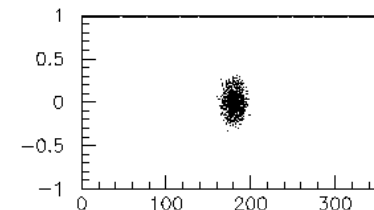
Source X-Y distribution



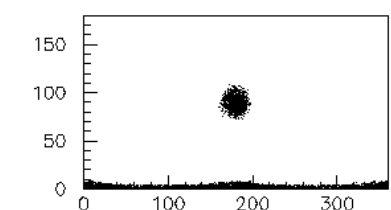
Source X-Z distribution



Source Y-Z distribution



Source cos(theta)-phi distribution



Source theta/phi distribution

Interfaces to HEPevt and HepMC

- Interface implementations of G4VPrimaryGenerator to standard formats in HEP:
 - useful for experiment-specific primary generator implementation
- G4HEPEvtInterface:
 - Suitable to /HEPEVT/ common block, which many of (FORTRAN) HEP physics generators are compliant to
 - ASCII file input (4-vectors from HEP generator code)
- More can be found in `geant4/examples/extended/eventgenerator`:
 - Showing an interface to HepMC
 - which a few new (C++) HEP physics generators are compliant to
 - Eg : Pythia
 - ASCII file input or direct linking to a generator through HepMC

Summary

- User must derive from **G4VUserPrimaryGeneratorAction** and
 - Implement **GeneratePrimaries(G4Event* anEvent)**
 - Register it to the run manager
 - Very recommended : use internally a **G4VPrimaryGenerator** for actual particle generation
 - If you implement your own generator, please start from this class.
- Generators must be derived from **G4VPrimaryGenerator**
 - Implementing **GeneratePrimaryVertex(G4Event* event)**
 - G4PrimaryVertex objects will be generated
 - To which G4PrimaryParticle objects will be associated
- Some built-in generators are provided:
 - **G4ParticleGun**, for simple cases
 - G4GeneralParticleSource for more complex ones
 - Interface G4HEPEvtInterface

For information : what happens then to your “primary particles” ?

- After MyPrimaryGeneratorAction:: GeneratePrimaries(G4Event* anEvent) call :
 - Geant4 makes the conversion :
 - G4PrimaryVertex + G4PrimaryParticle objects → G4Tracks objects
 - Remember, G4Track has:
 - particle type information : mass, charge, PDG, etc.
 - dynamic information : position, time, energy, momentum, polarization, etc.
 - And puts these tracks on the urgent (= normal) stack
 - More on stacks later : for now, it is a stack of particle waiting for being tracked
- Then, the event simulation starts :
 - the G4Track object on top of the stack is popped up and tracked in your detector representation
- Why G4PrimaryVertex and G4PrimaryParticle, and not directly G4Tracks in GeneratePrimaries(G4Event* anEvent) ?
 - G4Track is (too) specific to Geant4, with other information of no meaning for the generation
 - “G4TouchableHistory” geometrical information
 - Or pointer to a G4Step, etc.
 - G4PrimaryVertex and G4PrimaryParticle are free from this G4-specific stuff, and hence offer easier interfacing to standard particle and vertex representations
 - Like HEPevt, HEPMC, etc.